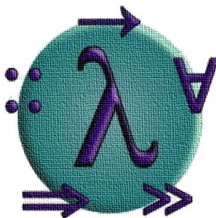


An overview of Haskell

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Outline

- 1 Introduction
 - Nice Syntactic Features
- 2 Features
 - Type System
 - Higher Order Functions
 - IO and Monads
 - Testing
- 3 Haskell Implementation
 - The Spineless Tagless G-Machine Language
 - Memory Representation
 - Running on Ordinary Machines
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Introduction

Haskell is a **pure functional language**. It means that:

- Variables never change after definition.
- Functions don't have side effects.
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History

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- (Nevertheless, it is an elegant language.)
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Named after Haskell B. Curry:



History

Designed by a committee



Nice syntactic features

Guards

- Standard if-then-else:

```
my_gcd1 m n = if n ≡ 0 then m  
              else if m < n then my_gcd1 n m  
              else my_gcd1 n (m 'mod' n)
```

- Guards:

```
my_gcd2 m 0 = m  
my_gcd2 m n | m < n = my_gcd2 n m  
              | otherwise = my_gcd2 n (m 'mod' n)
```

Nice syntactic features

Guards

- Standard if-then-else:

$$\begin{aligned} \text{my_gcd}_1 \ m \ n &= \text{if } n \equiv 0 && \text{then } m \\ &\text{else if } m < n && \text{then } \text{my_gcd}_1 \ n \ m \\ &\text{else } \text{my_gcd}_1 \ n \ (m \text{ 'mod' } n) \end{aligned}$$

- Guards:

$$\begin{aligned} \text{my_gcd}_2 \ m \ 0 &= m \\ \text{my_gcd}_2 \ m \ n \mid m < n &= \text{my_gcd}_2 \ n \ m \\ &\mid \text{otherwise} = \text{my_gcd}_2 \ n \ (m \text{ 'mod' } n) \end{aligned}$$

Nice syntactic features

Pattern Matching

- Simple Case expressions:

$$\begin{aligned} \text{factorial}_1 n &= \text{case } n \text{ of} \\ &0 \rightarrow 1 \\ &n \rightarrow n * \text{factorial}_1 (n - 1) \end{aligned}$$

- Pattern Matching:

$$\begin{aligned} \text{factorial}_2 0 &= 1 \\ \text{factorial}_2 n &= n * \text{factorial}_2 (n - 1) \end{aligned}$$

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Lists

A list in Haskell is defined recursively.

Definition

```
data [a] = [] | a : [a]
```

And there's some syntactic sugar for using lists:

```
[1..3] ≡ [1,2,3] ≡ 1 : [2,3] ≡ 1 : 2 : 3 : []
```

Lazy Lists

Since Haskell is a lazy language, you can define infinite lists:

```
primes = sieve [2..] where  
  sieve (p : tail) = let  
    filtered_tail = sieve [n | n ← tail, n `mod` p > 0]  
  in p : filtered_tail
```

```
factorial_list = 1 : [a * n | a ← factorial_list  
                       | n ← [1..]]
```


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```
factorial_list = 1 : [a * n | a ← factorial_list  
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```

QuickSort

```
quicksort [] = []  
quicksort (hd : tail) = quicksort small ++ [hd] ++ quicksort large  
where  
  small = [x | x ← tail, x ≤ hd]  
  large = [x | x ← tail, x > hd]
```

Currying

inc $x = 1 + x$

Currying

$$\text{inc } x = (+) 1 x$$

Currying

inc = (+) 1

Currying

inc = (+1)

Pointfree programming

$$h\ x = f\ (g\ (x))$$

Pointfree programming

$$h\ x = (f \cdot g)\ (x)$$

Pointfree programming

$$h = f . g$$

Type System Introduction

Haskell uses static typing, but is very expressive because of its polymorphism and type classes.

Example

```
reverse1 :: [a] → [a]
reverse1 [] = []
reverse1 (hd : tail) = reverse1 tail ++ [hd]
```

Since `reverse_list` is polymorphic, you can use it for any type of list:

- `reverse1 [1, 2, 3] → [3, 2, 1]`
- `reverse1 "Hello, World" → "dlroW ,olleH"`

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Algebraic Data Types

Haskell supports user defined algebraic data types, which combined with pattern matching are very expressive.

```
data Maybe a = Nothing | Just a
```

Example

```
divide :: (Integral a) => a -> a -> Maybe a  
divide x 0 = Nothing  
divide x y = Just (x 'div' y)
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Algebraic Data Types

Decomposition using pattern matching

Example

default_value :: **Maybe** a → a → a

default_value **Nothing** x = x

default_value (**Just** x) _ = x

Algebraic Data Types

Describing complex data structures

Complex data structures can be described (without pointers, of course).

```
data Tree a = Leaf a | Branch (Tree a) (Tree a)
```

```
size :: Tree a → Int
```

```
size (Leaf _) = 1
```

```
size (Branch left right) = 1 + size left + size right
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Encapsulation

There is no abstract type construct in Haskell, but instead there is a hierarchial module system, which can be used for encapsulation.

Example

```
module Stack (Stack, push, pop, empty,  
              top, is_empty) where  
  
data Stack a    = Stk [a]  
empty          = Stk []  
  
push (Stk s) x = Stk (x : s)  
pop (Stk (x : s)) = Stk s  
top (Stk (x : s)) = x  
is_empty (Stk s) = null s
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Type Classes

In Haskell, Type classes allow both overloading names, and writing generic functions which are made specific for some class.

Example

```
class Eq a where
```

```
( $\equiv$ ) :: a → a → Bool
```

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```
instance Eq Int where
```

```
  i1  $\equiv$  i2 = eqlnt i1 i2
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  i1  $\neq$  i2 = not (i1  $\equiv$  i2)
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instance Eq Int where
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Type Classes

Generic Classes and Functions

Example

instance ($Eq\ a$) \Rightarrow $Eq\ [a]$ **where**

$[] \equiv [] = True$

$(x : xs) \equiv (y : ys) = x \equiv y \ \&\& \ xs \equiv ys$

$xs \not\equiv ys = \mathbf{not} (xs \equiv ys)$

member $:: Eq\ a \Rightarrow a \rightarrow [a] \rightarrow Bool$

member $x\ [] = False$

member $x\ (y : ys) \mid x \equiv y = True$

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Generic Classes and Functions

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Higher Order Functions

Functions are first-class values, and can be passed to other functions.

Example

```
map :: (a → b) → [a] → [b]
map f []           = []
map f (head : tail) = (f head) : (map f tail)
```

```
inc :: (Num a) ⇒ a → a
```

```
(*3) :: (Num a) ⇒ a → a
```

```
map inc [1, 2, 3] ≡ [2, 3, 4]
```

```
map (*3) [1, 2, 3] ≡ [3, 6, 9]
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map - More Uses

```
toUpper :: Char → Char  
map toUpper "Hello" ≡ "HELLO"
```

You can even define:

```
stringToUpper :: String → String  
stringToUpper = map toUpper
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IO and Monads

Pure functional language \Rightarrow No side-effects in functions.

So how can we perform IO?

With the IO Monad!

A value of the type **IO** *a* represent an action, which returns a value of type *a*, once performed.

Example

```
getLine :: IO String  
putStr  :: String  $\rightarrow$  IO ()
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Example

```
getLine :: IO String  
putStrLn :: String  $\rightarrow$  IO ()
```

IO Syntax

Example

```
greet :: String → String  
greet name = "Hello, " ++ name  
main :: IO ()  
main = do  
  name ← getLine  
  putStrLn (greet name)
```

Monadic Pointfree Syntax

Example

```
echo :: IO ()  
echo = putStr "> " >>  
      getLine   >>=  
      putStr    >>  
      putStr "\n"
```

▶ The Monad Type Class

The Maybe Monad

Maybe

```
f :: Int → Maybe Int
complex_function :: Maybe Int → Maybe Int
complex_function mint = do
  i1 ← mint
  i2 ← f i1
  return i2
```

The List Monad

List

$$(\times) :: [a] \rightarrow [b] \rightarrow [(a, b)]$$
$$xs \times ys = \mathbf{do}$$
$$x \leftarrow xs$$
$$y \leftarrow ys$$
$$\mathbf{return} (x, y)$$

Example

$$[1, 2] \times [3, 4] \rightarrow [(1, 3), (1, 4), (2, 3), (2, 4)]$$

Parsing

Parsec

```
perl_variable = do
  sigil ← oneOf "&$@%"
  name ← many alphaNum
  return (sigil : name)
```

Example

- `parse perl_variable "Parser" "$var" → Right "$var"`
- `parse perl_variable "Parser" "not a var" → Left "Parser" (line 1, column 1) : unexpected "n"`

GUI - Gtk2Hs

```
main_gui :: IO ()
main_gui = do
  initGUI
  window ← windowNew
  button  ← buttonNew
  set window [containerBorderWidth := 10,
              containerChild := button]
  set button [buttonLabel := "Hello World"]
  onClicked button (putStrLn "Hello World")
  onDestroy window mainQuit
  widgetShowAll window
  mainGUI
```



Testing with QuickCheck

```
property_factorial1 n =  
  factorial1 (n + 1) 'div' factorial1 n ≡ n + 1
```

```
quickCheck property_factorial1  
results in
```

```
*** Exception: stack overflow
```

```
property_factorial2 n = n ≥ 0 ==>  
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quickCheck property_factorial2  
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OK, passed 100 tests.
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Some more QuickCheck examples

$$\text{property_gcd } n = n \geq 0 \implies (n \text{ 'mod' } (\text{my_gcd}_2 \ n \ (n + 2))) \equiv 0$$

Checking only specific values:

$$\begin{aligned} \text{property_primes} &= \text{forAll } (\text{two some_primes}) \$ \lambda(p, q) \rightarrow \\ & (p \equiv q \parallel \text{gcd } p \ q \equiv 1) \\ & \text{where some_primes} = \text{elements } \$ \text{take } 200 \ \text{primes} \end{aligned}$$

Lists can be generated too:

$$\begin{aligned} \text{property_reverse } list &= (\text{reverse}_1 . \text{reverse}_1) \ list \equiv list \\ \text{property_quicksort } list &= \text{quicksort } list \equiv \text{List.sort } list \end{aligned}$$

Some more QuickCheck examples

$property_gcd\ n = n \geq 0 \implies (n \text{ 'mod' } (my_gcd_2\ n\ (n + 2))) \equiv 0$

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Lists can be generated too:

$property_reverse\ list = (reverse_1 . reverse_1)\ list \equiv list$
 $property_quicksort\ list = quicksort\ list \equiv List.sort\ list$

What else?

- Implementations: GHC, Hugs, Helium, JHC, YHC
- Parallel GHC, Concurrent GHC, STM
- Cabal
- Visual Haskell, EclipseFP
- Famous Projects Using Haskell: Pugs, Darcs.
- DSLs, DSELS.
- Literate Haskell

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Few Implementation Notes

- These notes are based on the article about the “Spineless Tagless G-Machine” by Simon Peyton Jones, which is the basis for current implementations of the Glasgow Haskell Compiler - GHC.
- I'll only speak about some of the basic details, because I have much more to learn ...

The Compiler Structure

- 1 Preprocessing - Removing the literate markup, if needed, and also running a C preprocessor, if asked by the user.
- 2 Compiling into the smaller *Core* language, an intermediate language without the syntactic sugar. Type checking is performed, and pattern matching is translated into simple **case** expressions.
- 3 Some optimizations are performed on the intermediate language.
- 4 The Core language is translated into the STG language.
- 5 The STG language is translated by a code generator into C, or into machine code.

We'll focus on the STG language, and how it is translated into C.

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The Spineless Tagless G-Machine Language

The STG language is a very austere functional language, or a subset of Haskell.

It contains only the following constructs:

- Function applications, for using functions.
- `let` and λ expressions, for creating new bindings.
- `case` expressions, for evaluating expressions.
- Constructor applications, for defining values.

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Translation into STG

Example

$$\begin{aligned} \text{map } f [] &= [] \\ \text{map } f (\text{head} : \text{tail}) &= (f \text{ head}) : (\text{map } f \text{ tail}) \end{aligned}$$

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Example

```
map f []           = []  
map f (head : tail) = (f head) : (map f tail)
```

is translated to

```
map = {} λn { head, list } →  
  case list of  
    Nil {}           → Nil {}  
    Cons { head, tail } →
```

Translation into STG

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is translated to

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Memory Representation

Many kinds of values:

- Functions: $\{ free_list \} \lambda n \{ arg_list \} \rightarrow expr$
Contain code, and pointers to their free variables.
- Thunks: $\{ free_list \} \lambda u \{ \} \rightarrow expr$
Unevaluated expressions, contain the code to evaluate, and any needed pointer.
- Constructors: $Constructor \{ arg_list \}$
Contain the pointers to the constructors' parameters, which might be functions or thunks themselves.
- Primitive Values:
Integers, characters, floating point numbers, etc.

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Closures

In a polymorphic language, you cannot always know statically if a pointer is a function or a thunk, for example:

$$\text{compose } f \ g \ x = f (g \ x)$$

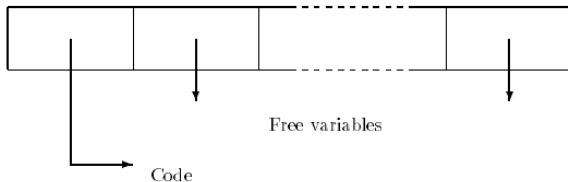
$g \ x$ might be a function or a thunk, on every call to `compose`. It is convenient to hold all values (except the primitives) in memory in the same structure, as **closures**:

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A mapping to ordinary machines

The STG language was defined with operational semantics. Each language construct has an operational meaning:

Construct	Operational meaning
Function application	Tail call
Let expression	Heap allocation
Case expression	Evaluation
Constructor application	Return to continuation

The STG Abstract Machine

The abstract machine which the implementation is based on has:

- Argument stack - a stack for passing parameters to functions.
- Return stack - a stack for continuations.
- Update stack - a stack for update frames (updating thunks).

The machine also includes a heap (garbage collected) for holding closures.

This is only the abstract machine, which is easier to understand. The real implementation has a different representation for these stacks.

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A function call is implemented by

- Pushing its arguments to the argument stack.
- Tail-calling the function (A jump into the function's code).

Example

```
map { f, tail }
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Let expressions

let expressions give local names to closures, and evaluate an expression in the local environment.

They are implemented by:

- Constructing the closures in the heap.
- Evaluating the expression

Example

```
let f_head = { f, head }  $\lambda u\{ \}$   $\rightarrow f\{y\}$   
    map_tail = { f, tail }  $\lambda u\{ \}$   $\rightarrow$  map{ f, tail }  
in Cons{ f_head, map_tail }
```

Case expressions

case expressions force evaluation of an expression, and then choose from alternatives based on its value.

They are implemented by:

- Pushing a continuation (or continuations) onto the return stack.
- Evaluate the expression.
- The evaluation is responsible for continuing according to the right alternative.

Example

```
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Constructor Applications

The application of a constructor is evaluated from within some case expression. The implementation:

- Pop the continuation from the return stack.
- Jump to the right alternative.

After return, either:

- a special register points to the constructor's closure, for the inspecting its values, or
- they could be returned in registers directly.

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Updating Thunks

In order to update thunks after they are evaluated:

- 1 When entering an updatable closure
 - An *update frame* is pushed to the update stack, which contain a pointer to the closure to be updated, and the contents of the arguments and return stacks.
 - The return stack and argument stack are made empty.
 - Its sometimes nice to update the closure temporarily with a “black hole” closure.
- 2 When evaluation of a closure is complete an update is triggered.
 - If the closure is a function, it won't find enough arguments on the argument stack.
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- 3 The update is either in-place, or by an indirection closure which is removed by GC.

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Links



<http://haskell.org>



Learning Haskell

Audrey Tang

<http://perlcabal.org/~autrijus/osdc/haskell.xul>



The Evolution of a Haskell Programmer

Fritz Ruehr

[http:](http://www.willamette.edu/~fruehr/haskell/evolution.html)

[//www.willamette.edu/~fruehr/haskell/evolution.html](http://www.willamette.edu/~fruehr/haskell/evolution.html)



A history of haskell: being lazy with class.

<http://research.microsoft.com/~simonpj/papers/history-of-haskell/history.pdf>

Links

Implementation



GHC Commentary

<http://hackage.haskell.org/trac/ghc/wiki/Commentary>



Implementing lazy functional languages on stock hardware: The spineless tagless g-machine.

<http://citeseer.ist.psu.edu/peytonjones92implementing.html>.



GHC Hackathon Videos

<http://video.google.com/videosearch?q=GHC+Hackathon&so=0>

Thank you!

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Questions?

Appendix

- 5 Appendix
 - An Efficient Reverse
 - Monad Class

An Efficient Reverse

By the way: The previous slide's $reverse_1$ function has $O(n^2)$ complexity, since each $++$ operation is linear in the first list's length. A more efficient version is:

```
reverse_2 :: [a] → [a]
reverse_2 list = helper list []
  where
    helper []      reversed = reversed
    helper (hd : tail) reversed = helper tail (hd : reversed)
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which runs in $O(n)$ complexity.

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Monad Class

class Monad *m* **where**

$(\gg=)$ $:: \forall a b . m a \rightarrow (a \rightarrow m b) \rightarrow m b$

(\gg) $:: \forall a b . m a \rightarrow m b \rightarrow m b$

return $:: \forall a . a \rightarrow m a$

fail $:: \forall a . String \rightarrow m a$

▶ Back